

# Dynamics of volume-averaged intracellular $\text{Ca}^{2+}$ in a rat CNS nerve terminal during single and repetitive voltage-clamp depolarizations

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## Key points

- The intracellular concentration of free calcium ions ( $[\text{Ca}^{2+}]_i$ ) in a nerve terminal controls both transmitter release and synaptic plasticity.
- The rapid triggering of transmitter release depends on the local micro- or nanodomain of highly elevated  $[\text{Ca}^{2+}]_i$  in the vicinity of open voltage-gated  $\text{Ca}^{2+}$  channels, whereas short-term synaptic plasticity is often controlled by global changes in residual  $[\text{Ca}^{2+}]_i$ , averaged over the whole nerve terminal volume.
- Here we describe dynamic changes of such global  $[\text{Ca}^{2+}]_i$  in the calyx of Held – a giant mammalian glutamatergic nerve terminal, which is particularly suited for biophysical studies.
- We provide quantitative data on  $\text{Ca}^{2+}$  inflow,  $\text{Ca}^{2+}$  buffering and  $\text{Ca}^{2+}$  clearance.
- These data allow us to predict changes in  $[\text{Ca}^{2+}]_i$  in the nerve terminal in response to a wide range of stimulus protocols at high temporal resolution and provide a basis for the modelling of short-term plasticity of glutamatergic synapses.

**Abstract** Many aspects of short-term synaptic plasticity (STP) are controlled by relatively slow changes in the presynaptic intracellular concentration of free calcium ions ( $[\text{Ca}^{2+}]_i$ ) that occur in the time range of a few milliseconds to several seconds. In nerve terminals,  $[\text{Ca}^{2+}]_i$  equilibrates diffusionally during such slow changes, such that the globally measured, residual  $[\text{Ca}^{2+}]_i$  that persists after the collapse of local domains is often the appropriate parameter governing STP. Here, we study activity-dependent dynamic changes in global  $[\text{Ca}^{2+}]_i$  at the rat calyx of Held nerve terminal in acute brainstem slices using patch-clamp and microfluorimetry. We use low concentrations of a low-affinity  $\text{Ca}^{2+}$  indicator dye (100  $\mu\text{M}$  Fura-6F) in order not to overwhelm endogenous  $\text{Ca}^{2+}$  buffers. We first study voltage-clamped terminals, dialysed with pipette solutions containing minimal amounts of  $\text{Ca}^{2+}$  buffers, to determine  $\text{Ca}^{2+}$  binding properties of endogenous fixed buffers as well as the mechanisms of  $\text{Ca}^{2+}$  clearance. Subsequently, we use pipette solutions including 500  $\mu\text{M}$  EGTA to determine the  $\text{Ca}^{2+}$  binding kinetics of this chelator. We provide a formalism and parameters that allow us to predict  $[\text{Ca}^{2+}]_i$  changes in calyx nerve terminals in response to a wide range of stimulus protocols. Unexpectedly, the  $\text{Ca}^{2+}$  affinity of EGTA under the conditions of our measurements was substantially lower ( $K_D = 543 \pm 51$  nM) than measured *in vitro*, mainly as a consequence of a higher than previously assumed dissociation rate constant ( $2.38 \pm 0.20$  s<sup>-1</sup>), which we need to postulate in order to model the measured presynaptic  $[\text{Ca}^{2+}]_i$  transients.

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**Abbreviations**  $[Ca^{2+}]_{rest}$ , resting intracellular free  $[Ca^{2+}]$ ; 4-AP, 4-aminopyridine; aCSF, artificial cerebrospinal fluid; AP, action potential; APW, action potential-like waveform;  $I_{Ca}$ , voltage activated  $Ca^{2+}$  current; MNTB, medial nucleus of the trapezoid body; Na/CaX,  $Na^+/Ca^{2+}$  exchanger; NCKX2,  $K^+$ -dependent  $Na^+/Ca^{2+}$  exchanger 2; P, postnatal day;  $Q_{Ca}$ , charge flow associated with a voltage activated  $Ca^{2+}$  current; STP, short-term synaptic plasticity;  $V_h$ , holding potential;  $V_m$ , membrane potential.

## Introduction

Although the local nano- or microdomain intracellular concentration of free calcium ions  $[Ca^{2+}]_i$  is generally accepted to be the relevant parameter for triggering neurotransmitter release (for review see Eggermann *et al.* 2012), measuring the spatially averaged, global  $[Ca^{2+}]_i$  in nerve terminals has often been instrumental for studying  $Ca^{2+}$ -dependent processes, in particular those underlying short-term synaptic plasticity (Kamiya & Zucker, 1994; Zucker & Regehr, 2002; Müller *et al.* 2008; Neher & Sakaba, 2008). Measurements of  $[Ca^{2+}]_i$ , however, are faced with the problem that  $Ca^{2+}$ -sensing probes such as  $Ca^{2+}$  indicator dyes bind  $Ca^{2+}$  ions and thus necessarily are also  $Ca^{2+}$  buffers, which influence the amplitude and time course of  $[Ca^{2+}]_i$  transients (Neher, 1995; Müller *et al.* 2007; Matthews & Dietrich, 2015). Quite often the  $Ca^{2+}$  indicator dyes, when added at concentrations required for well-resolved signals, overwhelm the endogenous  $Ca^{2+}$  buffering capacity and may cause substantial distortions of the intrinsic  $[Ca^{2+}]_i$  signals occurring in unperturbed cells.

While such signal distortions have sometimes limited the use of indicator dyes for  $[Ca^{2+}]_i$  measurement,  $Ca^{2+}$  chelators are often applied intentionally to the cytosol (Smetters *et al.* 1999; Stosiek *et al.* 2003) to block  $Ca^{2+}$ -mediated effects or to probe their  $Ca^{2+}$  sensitivity. In particular, the comparison of effects of the slow  $Ca^{2+}$  chelator EGTA with those of the fast buffer BAPTA proved to provide valuable insight regarding the spatial coupling between  $Ca^{2+}$  sources and effectors of  $Ca^{2+}$  action (Fedchyshyn & Wang, 2005; Vyleta & Jonas, 2014; Keller *et al.* 2015; Nakamura *et al.* 2015).

Last but not least,  $[Ca^{2+}]_i$  signals are used as optical readouts of activity in neuronal networks. The time resolution of such measurements is limited, however, due to the intrinsic  $[Ca^{2+}]_i$  dynamics, which are usually in the range 10–100 ms.

Given the multitude of presynaptic regulatory pathways that are controlled by  $[Ca^{2+}]_i$ , it is important to have reliable estimates at hand for the parameters which define the dynamics of global  $[Ca^{2+}]_i$  changes during presynaptic action potential (AP) firing. Such parameters are difficult to establish for small nerve terminals. Here we take advantage of the unique properties of a large mammalian glutamatergic nerve terminal – the calyx of Held – to

provide a detailed quantitative analysis of  $Ca^{2+}$  buffering and  $Ca^{2+}$  removal mechanisms, as well as an empirical description of  $Ca^{2+}$  currents during AP trains. Our results also reveal differences between  $Ca^{2+}$  dissociation and association rates of EGTA determined *in vitro* versus those determined in an intracellular environment. Given the role of EGTA as the ‘yardstick’ for estimating the spatial  $Ca^{2+}$  channel-vesicle coupling we would like to draw attention to this result.

Previous estimates of the parameters governing  $[Ca^{2+}]_i$  dynamics often depended on additional assumptions about the properties of  $Ca^{2+}$  indicator dyes and  $Ca^{2+}$  chelators, which had been obtained under different conditions and with different indicator dyes (Augustine *et al.* 1991; Neher & Augustine, 1992; Helmchen *et al.* 1997; Müller *et al.* 2007; McMahon *et al.* 2016). In particular, assumptions about the dissociation constant of  $Ca^{2+}$  indicator dyes vary widely in the literature. We therefore made an attempt to provide a set of parameters, which are internally consistent, all based on the  $Ca^{2+}$  indicator dye Fura-6F, which has been calibrated under exactly the same conditions as used in our experiments (Woehler *et al.* 2014). The low  $Ca^{2+}$  affinity of Fura-6F provides for minimum perturbation of the intrinsic  $[Ca^{2+}]_i$  signals and allows us to faithfully measure  $[Ca^{2+}]_i$  transients over a wide range of peak amplitudes (up to 30  $\mu M$ ).

## Methods

### Ethical approval

All experiments complied with the German Protection of Animals Act and with the guidelines for the welfare of experimental animals issued by the European Communities Council Directive. Experiments were performed on brain tissue from Wistar rats housed in the animal facility of the Max Planck Institute for Biophysical Chemistry. Rat pups were lightly anaesthetized using isoflurane (IsoFlo, Ecuphar, Germany) and killed by rapid decapitation.

### Slice preparation

Brainstem slices were prepared from Wistar rats of either sex at postnatal days (P) 8–10 (Fig. 1) or P13–15 (Figs 2–5) as previously described (Lin *et al.* 2011). Briefly, rat

pups were decapitated and the whole brain was quickly immersed into ice-cold low  $Ca^{2+}$  artificial cerebrospinal fluid (aCSF) containing (in mM): 125 NaCl, 2.5 KCl, 3  $MgCl_2$ , 0.1  $CaCl_2$ , 10 glucose, 25  $NaHCO_3$ , 1.25  $NaH_2PO_4$ , 0.4 ascorbic acid, 3 *myo*-inositol and 2 sodium pyruvate, pH 7.3. The brainstem was glued onto the stage of a VT1000S vibratome (Leica, Nussloch, Germany) and coronal slices (180–200  $\mu m$  thick) containing the medial nucleus of the trapezoid body (MNTB) were cut. Slices were incubated for  $\geq 30$  min at  $35^\circ C$  in an incubation chamber containing normal aCSF and kept at room temperature ( $22$ – $24^\circ C$ ) and used for experiments for up to 4 h thereafter. The composition of normal aCSF was identical to that of low  $Ca^{2+}$  aCSF except that 1.0 mM  $MgCl_2$  and 2.0 mM  $CaCl_2$  were used. All solutions were oxygenated by continuous equilibration with carbogen gas (95%  $O_2$ , 5%  $CO_2$ ).

## Electrophysiology

Patch-clamp recordings were made from calyx of Held terminals of the MNTB using an EPC-10 amplifier controlled by Pulse software (HEKA Elektronik, Lambrecht/Pfalz, Germany). Sampling intervals and filter settings were 20  $\mu s$  and 4.5 kHz, respectively. Cells were visualized by differential interference contrast microscopy through a  $60\times$  water-immersion objective (NA 1.0, Olympus, Hamburg, Germany) using an Axioskop FS microscope (Zeiss, Jena, Germany). All experiments were performed at room temperature.

Patch pipettes were pulled from borosilicate glass (Science Products GmbH, Hofheim, Germany) on a P-97 micropipette puller (Sutter Instrument, Novato, CA, USA). Pipettes were coated with dental wax to minimize fast capacitive transients during voltage-clamp experiments and to reduce stray capacitance. Open tip pipette resistance was 4–5  $M\Omega$  and access resistance ( $R_s$ ) values were  $\leq 20 M\Omega$ .  $R_s$  was routinely compensated for by 50–60% during presynaptic voltage-clamp experiments.

For measuring presynaptic  $I_{Ca}$ , pipettes were filled with a solution containing (in mM): 100 caesium gluconate, 30 tetraethylammonium chloride, 30 CsCl, 10 Hepes, 0.5 EGTA, 5  $Na_2$ -phosphocreatine, 4 ATP-Mg, 0.3 GTP, pH 7.3 with CsOH. We reported previously a  $Ca^{2+}$  contamination of typically 10–15  $\mu M$  and  $\sim 50 \mu M$  for nominally  $Ca^{2+}$ -free  $K^+$ -based and caesium gluconate-based pipette solutions, respectively (Woehler *et al.* 2014; their table 2). In this study, we supplemented pipette solutions with a minimum of 50  $\mu M$  EGTA to compensate for any  $Ca^{2+}$  contamination. For numerical simulations (see below), the resting intracellular free  $[Ca^{2+}]$  ( $[Ca^{2+}]_{rest}$ ) was assumed to be 20 or 50 nM for intracellular solutions containing 500 or 50  $\mu M$  EGTA, respectively. This is consistent with a total  $Ca^{2+}$  contamination in the tens of  $\mu M$  range.

The bath solution was supplemented with 1  $\mu M$  TTX, 1 mM 4-AP and 40 mM tetraethylammonium chloride to suppress voltage-gated sodium and potassium currents. The holding potential ( $V_h$ ) was set to  $-80$  mV for all presynaptic voltage-clamp recordings. No liquid junction potential corrections ( $< 10$  mV) were applied.

## Presynaptic $Ca^{2+}$ imaging

Presynaptic  $[Ca^{2+}]_i$  was monitored using the ratiometric  $Ca^{2+}$  indicator dye Fura-6F, which was excited at 350 and 380 nm by a monochromator (Polychrome 5, TILL Photonics, Gräfelfing, Germany). Fluorescence images were collected with an interline-transfer  $640\times 480$  pixel 12-bit monochrome cooled CCD camera (Imago, TILL Photonics) as previously described (Müller *et al.* 2007; Lin *et al.* 2012). To allow for brief exposure times, on-chip pixel binning ( $8\times 15$ ) was used. The monochromator and CCD camera were controlled by the TILLvisION software (TILL Photonics). Time series images were analysed off-line.

To increase the time resolution and to minimize photobleaching, single-wavelength imaging of the  $Ca^{2+}$ -sensitive fluorescence at 380 nm was applied at an acquisition rate of 100 Hz (Müller *et al.* 2007). Single wavelength images were preceded and followed by 20 images taken with dual excitation at wavelengths of 350 and 380 nm (10 images at each wavelength). These images were used to calculate  $F_{sum}$  as a substitute for the fluorescence signal recorded at the isosbestic point.  $F_{sum}$  is defined as

$$F_{sum} = F_{350} + \alpha \times F_{380} \quad (1)$$

where  $\alpha$  ( $= 0.229$ ) is the isocoefficient of Fura-6F for our setup. The isocoefficient  $\alpha$  can be found by searching for a constant that makes the sum of the measured background-corrected fluorescence  $F_{sum}$  independent of  $[Ca^{2+}]_i$  (Zhou & Neher, 1993).  $F_{sum}$  was calculated both from the initial 20 and final 20 images acquired at 350 and 380 nm. Linear interpolation was used to estimate the time course of  $F_{sum}$  during single-wavelength imaging. The background-corrected fluorescence signals were converted into  $[Ca^{2+}]_i$  using the following equation (Lee *et al.* 2000):

$$[Ca^{2+}]_i = K_{eff}(R' - (R_{min} + \alpha))/((R_{max} + \alpha) - R'), \quad (2)$$

where  $R'$  is the ratio  $F_{sum}/F_{380}$ .

The calibration constants  $R_{min}$  and  $R_{max}$  were obtained from *in vitro* measurements.

Using  $K_D$ ,  $R_{max}$ ,  $R_{min}$  and  $\alpha$ , it is then possible to calculate the effective dissociation constant  $K_{eff}$  of the indicator dye according to (Zhou and Neher, 1993):

$$K_{eff} = K_D \times (R_{max} + \alpha)/(R_{min} + \alpha) \quad (3)$$

(note that this equation is given incorrectly in Woehler *et al.* 2014; their eqn 10).

The  $K_D$  of Fura-6F was determined by a titration method using exactly the same solutions as used here for recordings with  $K^+$ -based pipette solution (17.8  $\mu M$ ; Woehler *et al.* 2014). We prefer this latter  $K_D$  estimate, because it does not rely on another calibration buffer (see Discussion). We therefore used a Fura-6F  $K_D$  of 17.8  $\mu M$  for converting measured fluorescence ratios into  $[Ca^{2+}]_i$  and in all subsequent evaluations, including calculation of the  $Ca^{2+}$  binding ratio  $\kappa_B$  of Fura-6F.

### Analysis of electrophysiological and imaging data

All off-line analysis was done with Igor Pro (WaveMetrics, Lake Oswego, OR, USA). Presynaptic recordings with a leak current  $> 100$  pA were excluded from the analysis. Values are given either as mean  $\pm$  SEM or else with error estimates, as discussed in the section on modelling.

### Modelling of $Ca^{2+}$ currents and changes in intracellular free $Ca^{2+}$

Given the thickness of the calyx terminal and the median distance between active zones, which are both about 400 nm (Meinrenken *et al.* 2002), local  $[Ca^{2+}]_i$  gradients between active zones after episodes of  $[Ca^{2+}]_i$  influx dissipate in about 3 ms (using Einstein's equation for mean displacement and an apparent diffusion coefficient of 220  $\mu m^2 s^{-1}$ , divided by  $\kappa_S$ ). To model such global, diffusively equilibrated  $[Ca^{2+}]_i$  transients, we follow standard procedures (Neher & Augustine, 1992; Helmchen *et al.* 1997), assuming that the presynaptic  $Ca^{2+}$ -specific current  $I_{Ca}$  injects  $Ca^{2+}$  into a spatially equilibrated accessible volume  $v$ . This causes a  $Ca^{2+}$  influx  $j_{in}$  of magnitude

$$j_{in} = -I_{Ca}/(2 \times F \times v), \quad (4)$$

where  $F$  is the Faraday constant and the flux is in units of  $mol l^{-1} s^{-1}$ . Note that this definition is different from standard use of the symbol  $j$ , which often measures flux in  $mol m^{-2}$ .

$Ca^{2+}$  clearance mechanisms (pumps and exchangers, see below) cause a  $Ca^{2+}$  extrusion of magnitude  $j_{ex}$ . The balance of total  $Ca^{2+}$  concentration  $[Ca^{2+}]_{tot}$  within a short interval  $\Delta t$  is thus:

$$\Delta[Ca^{2+}]_{tot} = (j_{in} - j_{ex}) \times \Delta t. \quad (5)$$

We consider two fast  $Ca^{2+}$  buffers: (i) a fixed low-affinity endogenous buffer, characterized by its  $Ca^{2+}$  binding ratio  $\kappa_S$ , and (ii) the  $Ca^{2+}$  indicator dye, an added buffer with  $Ca^{2+}$  binding ratio  $\kappa_B$  (Zhou & Neher, 1993). Both buffers are assumed to equilibrate with the free intracellular  $Ca^{2+}$  concentration  $[Ca^{2+}]_i$  within the time resolution of simulated traces ( $\Delta t = 1$  ms), such that the change in

free  $[Ca^{2+}]_i$  in the absence of 'slow' buffers is given by Neher & Augustine (1992):

$$\begin{aligned} \Delta[Ca^{2+}]_i &= \Delta[Ca^{2+}]_{tot}/(1 + \kappa_S + \kappa_B) \\ &= (j_{in} - j_{ex}) \times \Delta t/(1 + \kappa_S + \kappa_B) \end{aligned} \quad (6)$$

$\kappa_S$  and  $\kappa_B$  are calculated according to Zhou & Neher (1993) using two parameters each, namely their total concentrations and dissociation constants (see Table 2).

Furthermore, we consider the  $Ca^{2+}$  chelator EGTA as a slow buffer, which is added at various amounts to the pipette solution. EGTA is assumed to bind  $Ca^{2+}$  at one site in competition with very rapid binding of hydrogen ions. Therefore its kinetic parameters are 'apparent' ones, influenced by pH. A pH value of 7.2 is assumed throughout. The binding of EGTA to  $Ca^{2+}$  is characterized by three parameters: the total concentration of binding sites  $[EGTA]_{tot}$ , the apparent rate constant  $k_{E,Ca+}$  for  $Ca^{2+}$  binding and the rate constant  $k_{E,Ca-}$  for  $Ca^{2+}$  dissociation (see Table 1).

Presynaptic  $Ca^{2+}$  extrusion  $j_{ex}$  is represented in the model by two mechanistically distinct components: (i) a low-affinity Michaelis–Menten type removal  $j_{ex,MM}$ , representing  $Ca^{2+}$  ATPases and possibly contributions by mitochondrial  $Ca^{2+}$  uptake and (ii) a Hill-type  $Ca^{2+}$  extrusion mechanism  $j_{ex,Hill}$ .  $j_{ex,MM}$  is characterized by an initial slope  $\gamma$  of its  $Ca^{2+}$  dependence and a half-maximal concentration  $K_{D,MM}$ , according to

$$j_{ex,MM} = \gamma \times \frac{[Ca^{2+}]_i}{1 + \frac{[Ca^{2+}]_i}{K_{D,MM}}} \quad (7)$$

At medium  $[Ca^{2+}]_i$  ( $> 0.5 \mu M$ ),  $j_{ex,Hill}$ , which represents  $Na^+/Ca^{2+}$  exchangers ( $Na/CaX$ ) (Kim *et al.* 2005), starts to contribute appreciably to  $Ca^{2+}$  extrusion.  $j_{ex,Hill}$  is represented in the model by a Hill-type equation, according to

$$j_{ex,Hill} = j_{H,max} \times f_K \times \frac{1}{1 + \left( \frac{K_{D,H}}{[Ca^{2+}]_i} \right)^{n_H}} \quad (8)$$

Here,  $j_{H,max}$  is the maximum  $Ca^{2+}$  flux, generated by  $j_{ex,Hill}$ , and  $K_{D,H}$  together with the Hill coefficient  $n_H$  (constrained to 2) determine the  $Ca^{2+}$  sensitivity of  $Na/CaX$ . A scaling factor  $f_K$  is included to allow for a variable contribution of  $j_{ex,Hill}$  to the  $Ca^{2+}$  clearance, depending on the composition of the ionic milieu inside the presynaptic terminal (see below).

Finally, a constant  $Ca^{2+}$  leak influx  $j_{in,leak}$  is assumed to balance  $Ca^{2+}$  extrusion  $j_{ex,rest}$  that is operating at resting  $Ca^{2+}$  level ( $[Ca^{2+}]_{rest}$ )

$$j_{in,leak} = j_{ex,rest} = j_{ex,MM,rest} + j_{ex,Hill,rest} \quad (9)$$



**Table 1. Parameters that were derived from or used in the joint least-square fit**

Description	Symbol	Units	Value	Comment
<b>Michaelis–Menten-type <math>Ca^{2+}</math> clearance</b>				see eqn (7)
Low $[Ca^{2+}]_i$ slope	$\gamma$	$s^{-1}$	$230 \pm 13$	
Half-maximal $[Ca^{2+}]_i$	$K_{D,MM}$	M	$4.9 \pm 0.62 \times 10^{-5}$	
<b>Hill-type <math>Ca^{2+}</math> clearance</b>				see eqn (8)
Maximum flux	$j_{H,max}$	$M s^{-1}$	$3.22 \pm 0.82 \times 10^{-4}$	
$Ca^{2+}$ sensitivity	$K_{D,H}$	M	$5.16 \pm 1.3 \times 10^{-6}$	
Hill coefficient	$n_H$		2.0	fixed (Lee <i>et al.</i> 2007)
K-factor	$f_K$		1	for $Cs^+$ -based pipette solution (fixed)
			$4.79 \pm 1.02$	for $K^+$ -based pipette solution (variable)
<b>Slow buffers</b>				
Added [EGTA]	$[EGTA]_T$	M	$5 \times 10^{-5}$ and $5 \times 10^{-4}$	for 2 sets of experiments, pH 7.2
Apparent $Ca^{2+}$ binding rate constant	$k_{E,Ca+}$	$M^{-1} s^{-1}$	$4.38 \pm 0.17 \times 10^6$	
$Ca^{2+}$ dissociation rate constant	$k_{E,Ca-}$	$s^{-1}$	$2.38 \pm 0.20$	
Dissociation constant	$K_D$	M	$5.43 \pm 0.51 \times 10^{-7}$	
<b>General</b>				
Accessible cell volume	$v$	litres	$3.9 \pm 0.48 \times 10^{-13}$	mean $\pm$ SEM among synapses

The same parameter set was used for all traces during the least-squares fit and allowed to vary jointly.  $n_H$  and  $[EGTA]_T$  were constrained to the values given.  $I_{Ca}$  and  $v$  were determined independently by manual fits to  $I_{Ca}$  traces.

With these definitions, the fluxes can be calculated for a given  $[Ca^{2+}]_i$  and the conservation of total  $Ca^{2+}$  leads to the differential equation

$$\frac{d[Ca^{2+}]_i}{dt} = (j_{in} + j_{in,leak} - j_{ex,MM} - j_{ex,Hill} + \sum j_B) / (1 + \kappa_S + \kappa_B) \quad (10)$$

with  $\sum j_B$  representing the sum of ‘fluxes’ due to the binding reactions of slow buffers. We include here the possibility to add further slow buffers for future extensions of the model. For the case of EGTA and the net flux  $j_E$  associated with it, we use

$$j_E = k_{E,Ca-} \times [CaEGTA]_i - k_{E,Ca+} \times [Ca^{2+}]_i \times [EGTA]_i \quad (11)$$

Here  $[CaEGTA]_i$  and  $[EGTA]_i$  are intracellular concentrations of  $Ca^{2+}$ -bound EGTA and free EGTA, and  $k_{E,Ca+}$  and  $k_{E,Ca-}$  are the  $Ca^{2+}$  binding and unbinding rate constants of EGTA, respectively.

In the absence of slow buffers and for the simplest case of a single linear  $Ca^{2+}$  clearance mechanism with a slope  $\gamma$ , the  $[Ca^{2+}]_i$  transient after a bout of  $Ca^{2+}$  influx decays exponentially with a time constant  $\tau$  of (Helmchen *et al.* 1997):

$$\tau = (1 + \kappa_S + \kappa_B) / \gamma \quad (12)$$

For the general case, the differential eqn (10) was integrated using a 5th-order Runge–Kutta–Fehlberg algorithm as provided by Igor Pro (‘IntegrateODE’ routine with step size control set to a maximum relative error of  $10^{-5}$ ). Simultaneously, concentrations of  $Ca^{2+}$ -bound and  $Ca^{2+}$ -free slow buffers were integrated. For the case of EGTA the corresponding differential equations are:

$$\frac{d[CaEGTA]_i}{dt} = -j_E \quad (13)$$

$$\frac{d[EGTA]_i}{dt} = j_E \quad (14)$$

Initial values for  $[EGTA]_i$  and  $[CaEGTA]_i$  were calculated on the basis of the law of mass action, assuming a  $[Ca^{2+}]_{i,rest}$  as specified for the various cases in the Results section.

Dynamic changes in  $I_{Ca}$  were modelled at a temporal resolution of 1 ms with two dynamic variables  $y$  and  $z$  representing facilitation and inactivation, respectively. Although this approach does not allow us to capture the fine kinetic details of  $I_{Ca}$  activation and deactivation, its temporal resolution is sufficiently high to describe amplitude changes in  $Ca^{2+}$  influx that occur during either sustained or repetitive depolarizations over a tens of millisecond time window, as required for our  $[Ca^{2+}]_i$  modelling. The corresponding parameters  $\tau_y$ ,  $\tau_z$ ,  $y_{max}$ ,  $z_{min}$ ,  $y_{inc}$  and  $z_{dec}$  are listed in Table 2. Initial values of

**Table 2. General parameters that were not derived from least-square fits**

Description	Symbol	Units	Value	Comment
<b>General</b>				
Intracellular free $[Mg^{2+}]$	$[Mg^{2+}]_i$	M	$5 \times 10^{-4}$	
Resting intracellular free $[Ca^{2+}]$	$[Ca^{2+}]_{rest}$	M	$5 \times 10^{-8}$	for low $[EGTA]_i$
			$2 \times 10^{-8}$	for high $[EGTA]_i$
<b>Calcium current (P13–15)</b>				
Initial current	$I_{Ca,0}$	A	$-1.07 \pm 0.07 \times 10^{-9}$	mean
Duration of current flow	$\hat{\partial}$	s	$1 \times 10^{-3}$	depolarizing steps
			$3.22 \times 10^{-4}$	mature APW
			$4.83 \times 10^{-4}$	immature APW
<b>Facilitation parameter <math>y</math></b>				
Time constant	$\tau_y$	s	0.023	
Maximum value	$y_{max}$		1.56	
Increment	$y_{incr}$		0.47	
<b>Inactivation parameter <math>z</math></b>				
Time constant	$\tau_z$	s	0.11	
Minimum value	$z_{min}$		0.75	for low $[EGTA]_i$
			0.67	for high $[EGTA]_i$
Decrement	$z_{decr}$		0.032	
<b>Fast buffers</b>				
Total concentration of fixed endogenous		M	$8.44 \times 10^{-3}$	calculated to yield $\kappa_5 = 21.1$ at low $[Ca^{2+}]_i$
Dissociation constant of fixed endogenous	$K_D$	M	$4 \times 10^{-4}$	
Total concentration of $Ca^{2+}$ indicator dye		M	$10^{-4}$	
Dissociation constant of $Ca^{2+}$ indicator dye	$K_D$	M	$1.78 \times 10^{-5}$	Fura-6F (Woehler <i>et al.</i> 2014)

$y$  and  $z$  were set to 1 and  $I_{Ca,i}$  corresponding to stimulus  $i$  was calculated as the product of the initial current  $I_{Ca,0}$  with the respective time-dependent values  $y_i$  and  $z_i$ :

$$I_{Ca,i} = y_i \times z_i \times I_{Ca,0} \quad (15)$$

The latter were integrated simultaneously with the other dynamic variables (see eqns 10, 13, 14) according to

$$\frac{dy}{dt} = (1 - y)/\tau_y \quad (16)$$

$$\frac{dz}{dt} = (1 - z)/\tau_z \quad (17)$$

Values for  $y$  and  $z$  were incremented and decremented, respectively, at the times of AP-like waveforms with

$$\Delta y = y_{inc} \times \hat{\partial} \times (y_{max} - y) \times y \times z \quad (18)$$

$$\Delta z = z_{dec} \times \hat{\partial} \times (z_{min} - z) \times y \times z, \quad (19)$$

where  $\hat{\partial}$  denotes the duration of  $Ca^{2+}$  influx.

Integration according to eqns (10)–(19) was performed piecewise between episodes of presynaptic  $Ca^{2+}$  influx.

For AP-like stimuli,  $\hat{\partial}$  is the effective duration of an AP, as given in Table 2.  $\hat{\partial}$  was calculated as the ratio of  $Ca^{2+}$  current integral over  $I_{Ca,0}$ .

For longer step depolarizations, parameters  $y$  and  $z$  were incremented every 1 ms, using the same eqns (18) and (19) with  $\hat{\partial} = 1$  ms.

The joint integration of eqns (10)–(19) yielded the time courses of  $I_{Ca}$  and of all concentrations involved at a time resolution of 1 ms. Subsequently, we binned the modelled  $[Ca^{2+}]_i$  time course according to the temporal resolution of the  $Ca^{2+}$  imaging frames (10 or 20 ms), in order to obtain modelled  $[Ca^{2+}]_i$  transients with the same time resolution as the experimental ones for better comparison. This binning included a small time shift for perfect registry of the two signals.

### Procedures for parameter fitting

The overall strategy for determining the parameters of Table 1 is described in the first paragraph of the Results section. More specifically, we started with traces for which  $I_{Ca}$  data were available. By comparing experimental and modelled  $I_{Ca}$  we first determined the parameters  $I_{Ca,0}$  and those related to variables  $y$  and  $z$  by trial and error. We

arrived at a set of parameters (Table 2), which described all  $I_{Ca}$  traces for experiments with  $Cs^+$ -based pipette solution (Figs 2A, C, E, 4 and 5). Parameters describing  $I_{Ca}$  were kept constant for the subsequent steps of analysis.

Next we compared experimental  $[Ca^{2+}]_i$  transients with the binned modelled  $[Ca^{2+}]_i$  time courses and varied the parameter  $\nu$ , as well as the jointly variable parameters of Table 1 for a visually satisfying fit. Finally, we used a least-squares fitting routine to refine the fit and to enforce the same values of jointly varying parameters for all traces. A custom-written stochastic optimization strategy that involved elements of simulated annealing and a genetic algorithm was used to determine a set of those parameters (Table 1), which are expected to be the same for all traces, such as binding and unbinding rate constants of  $Ca^{2+}$  buffers. The optimization algorithm minimized the mean-square deviation of all modelled  $[Ca^{2+}]_i$  transients shown in Figs 2, 4 and 5 after normalization with respect to their means. The sections of the modelled and measured  $[Ca^{2+}]_i$ , considered for the minimization, were typically 0.8 s long starting at the onset of stimulation. In some measured  $[Ca^{2+}]_i$  transients, in particular when using  $K^+$ -based pipette solutions, we noticed small delayed rises in  $[Ca^{2+}]_i$ , which might be due to reversal of  $Ca^{2+}$  uptake into intracellular stores (Werth & Thayer, 1994). In these cases we reduced the time window for the simulation, as indicated in the respective figure legends. All fits shown used the 'master set' of parameters (Tables 1 and 2).

When performing least-squares fits we noticed that we often encountered closely spaced local minima, which had almost identical least-squares deviations, but somewhat different subdivision of the  $Ca^{2+}$  clearance between  $j_{ex,MM}$  and  $j_{ex,Hill}$ . Parameters for  $Ca^{2+}$  buffering by EGTA, on the other hand, were quite robust. To estimate confidence intervals, we determined the Hessian matrix by varying each of the parameters by  $\pm 10\%$  (Monahan, 2001). We used the diagonal elements  $c_{ii}$  of its inverse and the mean square deviation  $\varepsilon$  of the fit to calculate a standard error for parameter  $i$  as

$$\sqrt{3 \times e_{ii} \times \varepsilon / N} \quad (20)$$

where  $N$  is the number of data points used for the fit. The factor 3 accommodates the finding that data points are not independent, but typically correlated over a mean correlation length of  $\sim 3$  (as determined by the half-point of decay of the auto-covariance function of residuals). The resulting standard errors are typically larger than variations in parameters between local minima. They are in the range 4–9% for EGTA-related parameters and for  $\gamma$ , the low  $[Ca^{2+}]_i$  slope of  $j_{ex,MM}$ . For the other fitting parameters they are in the range 15–25%, however (see Table 1).

## Results

The aim of this study was to determine a set of internally consistent parameters, which would allow one to model changes in  $Ca^{2+}$  influx and volume-averaged, global  $[Ca^{2+}]_i$  at the calyx of Held nerve terminal in response to various stimulation patterns. The time resolution of our experimental measurements was determined by the maximum frame rate ( $100\text{ s}^{-1}$ ) of our imaging device.  $Ca^{2+}$  equilibrates diffusionally across the width of the calyx which is variable but mostly  $< 1\text{ }\mu\text{m}$  (Sätzler *et al.* 2002; Dondzillo *et al.* 2010) and between active zones within 3 ms (see Methods), such that our images report volume-averaged  $[Ca^{2+}]_i$ .

As described in the Methods and summarized in Tables 1 and 2, our formalism to model  $[Ca^{2+}]_i$  transients involves at least 21 parameters [3 general parameters, 7 for describing  $I_{Ca}$ , 6 for describing  $Ca^{2+}$  clearance mechanisms and 5 for describing  $Ca^{2+}$  buffers (EGTA and endogenous fixed buffers)]. Some of these parameters were determined by independent measurements (e.g.  $\kappa_s$ ) or were assumed to be known (resting  $[Ca^{2+}]_i$  and  $n_H$ ), while 16 remaining parameters had to be determined by simulation and curve fitting. Our strategy to handle as many parameters was as follows: we started by determining the  $Ca^{2+}$  binding ratio of fixed endogenous buffers (see next section). These measurements were done after wash-out of endogenous mobile buffers in the presence of various amounts of  $Ca^{2+}$  indicator dye as the only mobile buffer. They yielded estimates for the  $Ca^{2+}$  binding ratio of fixed endogenous buffers,  $\kappa_s$ , and for the decay time constant of  $[Ca^{2+}]_i$  in the absence of any mobile buffer. The two values together allowed us to calculate  $\gamma$ , the initial slope of the relationship between the  $Ca^{2+}$  extrusion rate constant and  $[Ca^{2+}]_i$  (see eqn 12). In a further analysis, we kept  $\kappa_s$  fixed and used  $\gamma$ , thus determined, as the starting value for the least-squares fitting procedure.

Next, we studied  $[Ca^{2+}]_i$  transients in calyx terminals that were dialysed with a  $Cs^+$ -based pipette solution containing  $100\text{ }\mu\text{M}$  Fura-6F and a low concentration of EGTA of  $50\text{ }\mu\text{M}$ . This allowed us to measure  $I_{Ca}$  and  $[Ca^{2+}]_i$  simultaneously and to determine parameters related to  $I_{Ca}$  and to the  $Ca^{2+}$  extrusion mechanisms by trial and error fitting. At this step, we used a first guess of parameters related to EGTA. Next, we performed similar experiments with the only difference that the concentration of EGTA was increased 10-fold to  $500\text{ }\mu\text{M}$ . This provided refined estimates for EGTA-related parameters. A few cycles of fits between this data set and the previous one converged onto a set of EGTA parameters, which we consider to be reliable at this stage of analysis. Next, we analysed an additional set of  $[Ca^{2+}]_i$  measurements that was obtained under whole-cell conditions with a pipette solution including  $K^+$  as the main cation. We added this experimental

condition because of the known major contribution of a  $K^+$ -sensitive Na/CaX to the  $Ca^{2+}$  extrusion at the calyx of Held (Lee *et al.* 2007b). To model  $[Ca^{2+}]_i$  transients that were measured with  $K^+$ -based pipette solutions, we kept all parameters determined so far fixed, except for the scaling factor  $f_K$  which determines the relative contribution of the  $K^+$ -sensitive Na/CaX to the total  $Ca^{2+}$  clearance. We found, indeed, that the contribution of Na/CaX increased strongly when using  $K^+$ -based pipette solutions.

Up to this point, all fitting was done manually by minimizing deviations between measured and modelled  $I_{Ca}$  and/or  $[Ca^{2+}]_i$  as judged by visual inspection. Next, however, we subjected the whole set of modelled  $[Ca^{2+}]_i$  transients to a non-linear, iterative optimization procedure with a jointly variable parameter set (Table 1; see Methods for details). We used the resulting 'master set' of parameters from here on. The model parameters are summarized in Tables 1 and 2.

### Evaluation of the $Ca^{2+}$ binding ratio of fixed endogenous buffers, $\kappa_s$

Estimates for the binding ratio  $\kappa_s$  of P8–10 calyces of Held range between 27 and 71 with an average of  $\sim 40$  (Helmchen *et al.* 1997). Babai *et al.* (2014) recently reported a somewhat higher value of 46. All these values were derived from  $[Ca^{2+}]_i$  transients recorded in response to short depolarizations while terminals were loaded with the high-affinity  $Ca^{2+}$  indicator dye Fura-2. However, using low-affinity indicators such as MagFura-2 and Calcium Orange-5N, Helmchen *et al.* (1997) found a  $\kappa_s$  of  $\sim 20$ . Estimates for  $\kappa$  obtained during dye loading may contain a contribution of mobile endogenous buffers, which slowly wash out while the indicator dye diffuses into the cell (Matthews & Dietrich, 2015). We therefore re-evaluated  $\kappa_s$  by loading calyx terminals with  $Cs^+$ -based pipette solutions containing various concentrations of the low-affinity indicator Fura-6F (100, 300 and 1000  $\mu M$ ) and evaluating  $[Ca^{2+}]_i$  transients in response to depolarizations, after dye loading had completed and the concentration of the indicator dye had reached steady state ( $\geq 3$  min after establishing whole cell configuration). At that time endogenous  $Ca^{2+}$  binding proteins, such as parvalbumin, should be substantially reduced in concentration, although not completely washed out.

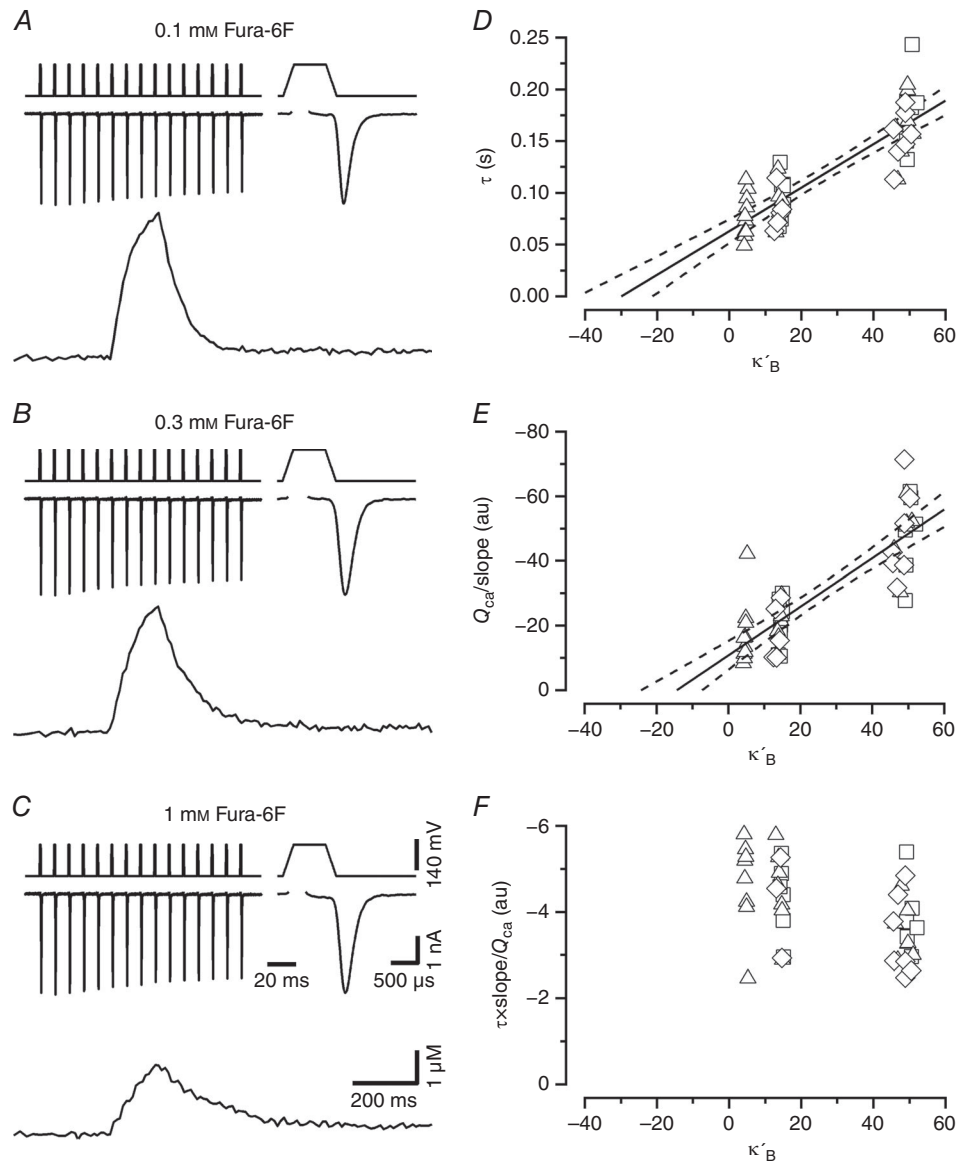
We applied 100 Hz trains consisting of 15 action potential-like waveforms (APWs) of variable durations to elicit short transients of  $I_{Ca}$  in the range  $-2$  to  $-4$  nA (Fig. 1A–C). This caused  $[Ca^{2+}]_i$  transients with amplitudes of 1.5–3  $\mu M$  when measured with 1 mM Fura-6F and between 3 and 5  $\mu M$  for lower concentrations of the indicator dye. We evaluated the current integrals  $Q_{Ca}$  and the  $[Ca^{2+}]_i$  transients caused by such  $Ca^{2+}$

influx.  $[Ca^{2+}]_i$  transients rose exponentially during trains and decayed exponentially afterwards (Fig. 1A–C; bottom traces). In Fig. 1D, the decay time constants  $\tau$  of the  $[Ca^{2+}]_i$  transients are plotted as a function of  $\kappa_B$ , the  $Ca^{2+}$  binding ratio of the indicator dye. The latter was calculated according to eqn (10) of Zhou & Neher (1993). The  $y$ -offset value ( $63 \pm 6$  ms) of a regression line to such a scatter plot is an estimate for the time constant of  $[Ca^{2+}]_i$  decay that would be obtained in the complete absence of indicator dye and any other mobile  $Ca^{2+}$  buffers. The negative  $x$ -axis intercept is an estimate for  $1 + \kappa_s$  (Neher & Augustine, 1992, their fig. 9). Likewise, another estimate of  $1 + \kappa_s$  can be obtained from the initial rate of rise  $s$  of the  $[Ca^{2+}]_i$  transients, which is proportional to  $Q_{Ca}/(1 + \kappa_s + \kappa_B)$  (Neher & Augustine, 1992; Helmchen *et al.* 1997). Thus, we also plotted  $Q_{Ca}/s$  against  $\kappa_B$  (Fig. 1E). Regression lines to both types of plots yielded  $\kappa_s$  values of 29.0 and 13.3. We used the mean of these two values (21.1) for the simulations described below. This value is lower than those determined previously. However, it is well in line with a consistency argument, put forward by Neher & Taschenberger (2013) and it may be more accurate, as it is based on a low-affinity  $Ca^{2+}$  indicator, avoiding possible influences of saturation, as well as problems due to incomplete washout of mobile buffers. Yet, the two estimates for  $\kappa_s$  yield quite different numbers. To explore possible sources for the discrepancy, we plotted the ratio of the two quantities shown in Fig. 1D and E (Fig. 1F). In this plot, the influence of buffers should be cancelled out, such that no dependence on  $\kappa_B$  is expected. However, the values for high  $\kappa_B$ , corresponding to the experiments with the highest Fura-6F concentration and lowest  $[Ca^{2+}]_i$  amplitudes, are significantly lower than the values obtained with lower Fura-6F concentrations. Possible reasons for these variations are discussed below.

### $[Ca^{2+}]_i$ dynamics in the near absence of mobile $Ca^{2+}$ buffers

In the near absence of mobile  $Ca^{2+}$  buffers, assuming that fixed buffers have a low  $Ca^{2+}$  affinity, small changes in  $[Ca^{2+}]_i$  should be well described by eqn (12), which in the low-concentration limit relates the decay time constant  $\tau$  of a  $[Ca^{2+}]_i$  transient to the  $Ca^{2+}$  binding ratio  $\kappa_s$  of endogenous fixed buffers and the quantity  $\gamma$ . Given the values for  $\kappa_s$  and  $\tau$  as determined in the last section one can calculate  $\gamma$  and thereby arrive at a complete kinetic description of this simplified scenario. It has been shown, however, that  $Ca^{2+}$  clearance mechanisms are quite complex, involving  $Ca^{2+}$  pumps, Na/CaXs and uptake into organelles (Lee *et al.* 2007b). Such contributions have non-linear characteristics and set in at  $[Ca^{2+}]_i$  above 0.5–1  $\mu M$ . To explore the  $[Ca^{2+}]_i$  dynamics in the range  $\geq 1$   $\mu M$ , we performed a series of experiments using depolarizing voltage-clamp steps to a membrane potential





**Figure 1. Evaluation of the  $Ca^{2+}$  binding ratio  $\kappa_s$  of endogenous fixed  $Ca^{2+}$  buffers**

A–C, example traces of presynaptic  $I_{Ca}$  (top) together with the corresponding  $[Ca^{2+}]_i$  transients (bottom) elicited by stimulus trains and recorded in calyx of Held terminals. The first  $I_{Ca}$  waveform of the trains is shown at a faster time scale (top right) in the top row of each panel. Voltage-clamp protocols are shown above  $I_{Ca}$ . Stimulus trains consisted of 15 APW depolarizations delivered at a frequency of 100 Hz. APWs consisted of a variable length depolarization to +60 mV (0.2, 0.6 or 1 ms) embedded in two ramps of 0.2 ms duration (from –80 to +60 mV and from +60 to –80 mV). Terminals were loaded with either 0.1 mM (A), 0.3 mM (B) or 1 mM (C) Fura-6F. For the sample traces shown, peak  $[Ca^{2+}]_i$  was  $4.60 \mu$ M (A),  $4.02 \mu$ M (B) and  $2.28 \mu$ M (C). Calibration bars in C also apply to A and B. D, decay time constants of the  $[Ca^{2+}]_i$  transients plotted versus the  $Ca^{2+}$  binding ratios  $\kappa'_B$  of Fura-6F for  $I_{Ca}$  evoked by 0.2 ms (squares), 0.6 ms (triangles) and 1 ms (diamonds) APWs. Pooled data obtained from 10 (0.1 mM Fura-6F), 8 (0.3 mM Fura-6F) and 7 (1 mM Fura-6F) calyx terminals. The data are clustered along the x-axis, with each cluster corresponding to one of the three Fura-6F concentrations used (0.1 mM left, 0.3 mM middle, 1 mM right). The x-values within clusters scatter slightly due to differences in peak amplitudes of the respective  $[Ca^{2+}]_i$  transients. A line fit to the data yields a  $\kappa_s$  estimate of  $29.0 \pm 4.9 \mu$ M. E, when plotting the ratio  $Q_{Ca}$  over initial rate of rise of the  $[Ca^{2+}]_i$  transients in a similar way as shown in D, the estimated  $\kappa_s$  amounts to  $13.3 \pm 4.1 \mu$ M. Solid and broken lines in D and E represent regression lines and 95% confidence limits, respectively. Error estimates for  $\kappa_s$  values were derived from bootstrap analysis using a resampling  $n$  of 10,000. F, the ratio of the two quantities shown in D and E is plotted. This ratio should be independent of  $\kappa'_B$ , since the influence of the latter is cancelled out. This holds for the comparison of values obtained with 0.1 and 0.3 mM Fura-6F. However, the mean value for the data obtained with 1 mM Fura-6F in the pipette ( $-3.10 \pm 0.15 \times 10^6$ ) is slightly smaller than the mean of the pooled data using 0.1 or 0.3 mM Fura-6F ( $-4.29 \pm 0.19 \times 10^6$ ).

yielding large  $I_{Ca}$  ( $V_m = 0$  mV). These experiments were performed in calyx terminals, which were dialysed with either  $Cs^+$ -based or  $K^+$ -based pipette solutions. Under the former conditions, we recorded the isolated  $I_{Ca}$  together with the volume-averaged  $[Ca^{2+}]_i$  transient. In each case, we included low concentrations of EGTA ( $50 \mu M$ ) and  $Ca^{2+}$  indicator ( $100 \mu M$  Fura-6F) in the pipette solution (see Methods for exact composition) and applied depolarizing voltage pulses of 10, 30 and 50 ms duration. At such low concentrations of  $Ca^{2+}$  buffer, the resting  $[Ca^{2+}]_i$  level is determined by  $Ca^{2+}$  clearance mechanisms and by  $Ca^{2+}$  contamination in the nominal  $Ca^{2+}$ -free pipette solution ( $\sim 50 \mu M$ ; Woehler *et al.* 2014). Since the low-affinity indicator dye does not allow accurate measurements of  $[Ca^{2+}]_i$  in the expected range of values, we assumed a basal  $[Ca^{2+}]_i$  of 50 nM in this type of experiment and adjusted the baselines for both modelled and measured  $[Ca^{2+}]_i$  traces accordingly.

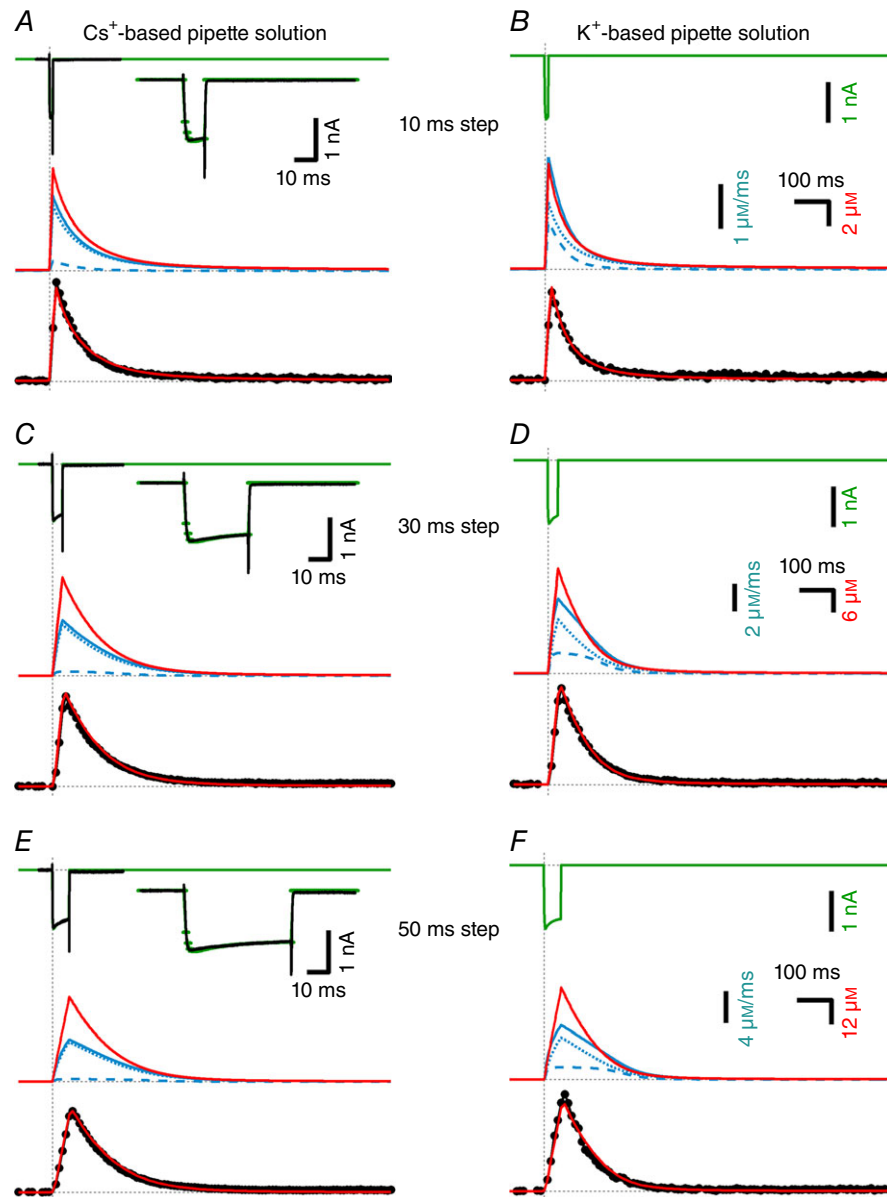
Figure 2 shows examples of  $[Ca^{2+}]_i$  transients (bottom traces) and  $I_{Ca}$  (top traces) evoked by step depolarizations of three different durations and recorded with  $Cs^+$ -based (Fig. 2A, C, E) or with  $K^+$ -based (Fig. 2B, D, F) pipette solution. In all cases, the 10 ms binned modelled  $[Ca^{2+}]_i$  transients obtained with the 'master set' of fitting parameters are superimposed.  $[Ca^{2+}]_i$  model traces (red) and  $Ca^{2+}$  clearance rates (blue) are shown in the middle of panels at full time resolution. Close inspection of the  $[Ca^{2+}]_i$  transients recorded with  $K^+$ -based pipette solutions shows that these decay faster compared to those recorded using  $Cs^+$ -based pipette solutions under otherwise identical conditions (compare left vs. right panels in Fig. 2). Exponential fits to the decays of  $[Ca^{2+}]_i$  transients elicited by 10 ms steps yield time constants of  $79.1 \pm 1$  and  $61 \pm 2$  ms for experiments using  $Cs^+$ -based and  $K^+$ -based pipette solutions, respectively. Corresponding time constants for 30 ms steps are  $102 \pm 0.5$  and  $78.7 \pm 0.8$  ms, and for 50 ms steps they are  $104.9 \pm 0.5$  and  $72.7 \pm 1$  ms. This result is in line with previous work establishing the  $K^+$  dependence of the  $Ca^{2+}$  clearance via Na/CaXs (Lee *et al.* 2002; Kim *et al.* 2005). We modelled this situation by assuming a  $Ca^{2+}$  clearance mechanism with two components. The first component was a saturating Michaelis–Menten type mechanism ( $j_{ex,MM}$ ), representing Ca-ATPases and possibly some  $Ca^{2+}$  uptake into mitochondria (eqn 7). It was initialized in the fitting procedure to an initial slope of  $\gamma$  at low  $[Ca^{2+}]_i$  as determined above and an arbitrarily selected maximum contribution. Estimates for these parameters were initially improved by trial-and-error fits. The second component was a Hill-type non-linear mechanism ( $j_{ex,Hill}$ ) with a Hill coefficient  $n_H$  constrained to 2 (Lee *et al.* 2007b) and with two free parameters determining maximum rate ( $j_{max,H}$ ) and  $Ca^{2+}$  affinity ( $K_{D,H}$ ) (eqn 8). To model experimental data obtained with  $K^+$ -based pipette solutions, we scaled the latter

component with a multiplier  $f_K$  which was a free fitting parameter. It was, however, constrained to the same value for all  $[Ca^{2+}]_i$  transients obtained with  $K^+$ -based pipette solution. A subsequent least-squares fitting procedure (see Methods) converged to the parameters listed in Table 1. In particular, it yielded a value of  $4.79 \pm 1.02$  for  $f_K$ , indicating that  $j_{ex,Hill}$  is nearly five-fold higher when using  $K^+$ -based instead of  $Cs^+$ -based pipette solution. This is in excellent agreement with Lee *et al.* (2007a), who found that reverse mode NCKX2 currents were 5 times higher in  $K^+$ -based solutions as compared to  $Cs^+$ -based ones.

In Fig. 3 the rates for the total  $Ca^{2+}$  extrusion  $j_{ex}$  are plotted as functions of  $[Ca^{2+}]_i$  for both pipette solutions (continuous lines). In addition, the individual components  $j_{ex,MM}$  (green dotted line; identical for  $Cs^+$ - and  $K^+$ -based pipette solution) and  $j_{ex,Hill}$  (blue dotted line; for  $K^+$ -based pipette solution) are shown. With  $Cs^+$ -based pipette solution, total clearance rates are just marginally higher than those of  $j_{ex,MM}$  alone. However, for experiments using  $K^+$ -based pipette solutions clearance rises much faster between 1 and  $5 \mu M$  due to the higher contribution of  $j_{ex,Hill}$ . Figure 3 also shows linear approximations for  $j_{ex}$  in the low  $[Ca^{2+}]_i$  range (1 and  $5 \mu M$ ). Line fits are constrained to pass through the origin. For the  $Cs^+$ -based pipette solution, the initial slope is  $242 s^{-1}$ , only slightly larger than the parameter  $\gamma$  ( $= 230 \pm 13 s^{-1}$ ), as determined by the least-squares fit. Deviations between that line and the total  $Ca^{2+}$  clearance (red) are minor for  $[Ca^{2+}]_i \leq 10 \mu M$  because the sigmoidally increasing  $j_{ex,Hill}$  compensates for the beginning saturation of  $j_{ex,MM}$ . Thus, for experiments using  $Cs^+$ -based pipette solution, a linear clearance mechanism with a slope  $\gamma = 242 s^{-1}$  is a very good approximation of the total  $Ca^{2+}$  extrusion for  $[Ca^{2+}]_i \leq 10 \mu M$ , which largely covers the physiologically relevant range of  $[Ca^{2+}]_i$ .

With  $K^+$ -based pipette solutions, the larger contribution of  $j_{ex,Hill}$  leads to a steeper slope ( $349 s^{-1}$ ) for the line fit, although not changing the very initial slope of the model curve. Thus, the  $Ca^{2+}$  extrusion in response to  $[Ca^{2+}]_i$  elevations with small amplitudes, as generated by single APs (typically  $0.3$ – $0.5 \mu M$ ), has similar kinetics when using either  $Cs^+$ - or  $K^+$ -based pipette solution. The  $Ca^{2+}$  extrusion following higher  $[Ca^{2+}]_i$  elevations as typically observed during high frequency AP trains (in the range  $1$ – $5 \mu M$ ), however, is well approximated by a linear clearance with a rate constant of  $349 s^{-1}$  (the slope of the line fit) when using  $K^+$ -based pipette solution.

The linear approximation discussed here, together with the value of  $\kappa_s$  as determined above, allows one to predict decay time constants of  $[Ca^{2+}]_i$  transients after mild stimulation and in the absence of mobile buffers according to eqn (12). For small AP-evoked signals we predict  $\tau = 22.1/242 s^{-1} = 91$  ms for both  $Cs^+$ - and  $K^+$ -based



**Figure 2. Time course of  $[Ca^{2+}]_i$  transients in the near absence of mobile  $Ca^{2+}$  buffers using either  $Cs^+$ - or  $K^+$ -based pipette filling solutions**

In each panel, measured  $[Ca^{2+}]_i$  transients (black, bottom) in response to depolarizing voltage-clamp pulses are compared with the modelled  $[Ca^{2+}]_i$  (red, middle and bottom). Patch pipettes contained  $50 \mu M$  EGTA and  $100 \mu M$  Fura-6F in all experiments illustrated. *A*, top,  $I_{Ca}$  (black) evoked by a depolarizing voltage step (10 ms to 0 mV) was measured with  $Cs^+$ -based pipette solution and is shown superimposed onto the modelled  $I_{Ca}$  (green). The inset shows measured and modelled  $I_{Ca}$  at a faster time scale. Middle, modelled  $[Ca^{2+}]_i$  transient (red trace) and  $Ca^{2+}$  extrusion rate  $j_{ex}$  (solid blue trace) and its components  $j_{ex,Hill}$  (blue broken trace) and  $j_{ex,MM}$  (blue dotted trace) are shown at high temporal resolution ( $\Delta t = 1$  ms). Bottom, modelled (red) and measured (black)  $[Ca^{2+}]_i$  transients shown superimposed. The modelled  $[Ca^{2+}]_i$  transient was binned using 10 ms time intervals that were shifted for optimal alignment with the measured trace. *C* and *E*, data obtained from the same calyx terminal during similar experiments as shown in *A* except that the durations of the depolarizing voltage steps were 30 ms (*C*) and 50 ms (*E*). The measured peak  $[Ca^{2+}]_i$  was  $8.06 \mu M$  (*A*),  $24.4 \mu M$  (*C*) and  $40.3 \mu M$  (*E*). *B*, *D* and *F*, similar experiments as illustrated in *A*, *C* and *E* but using  $K^+$ -based pipette solution. Since  $I_{Ca}$  could not be recorded in isolation under these experimental conditions, only the modelled  $I_{Ca}$  (green) is shown. The measured peak  $[Ca^{2+}]_i$  was  $7.16 \mu M$  (*B*),  $26.0 \mu M$  (*D*) and  $47.7 \mu M$  (*F*). The least-squares fits to the data shown in *A*, *C* and *E* used 80 data points of the sampled  $[Ca^{2+}]_i$  transient, starting at onset of the presynaptic depolarization and ending 0.8 s later. The fit to the data shown in *B* used 37 data points and the fits to the data shown in *D* and *F* used 60 data points.

pipette solution, while for  $[\text{Ca}^{2+}]_i$  transients elicited by high frequency trains we expect a value similar to that with  $\text{Cs}^+$ -based pipette solution, but a faster one ( $\tau = 22.1/349 \text{ s}^{-1} = 63 \text{ ms}$ ) for experiments using  $\text{K}^+$  as the main internal cation.

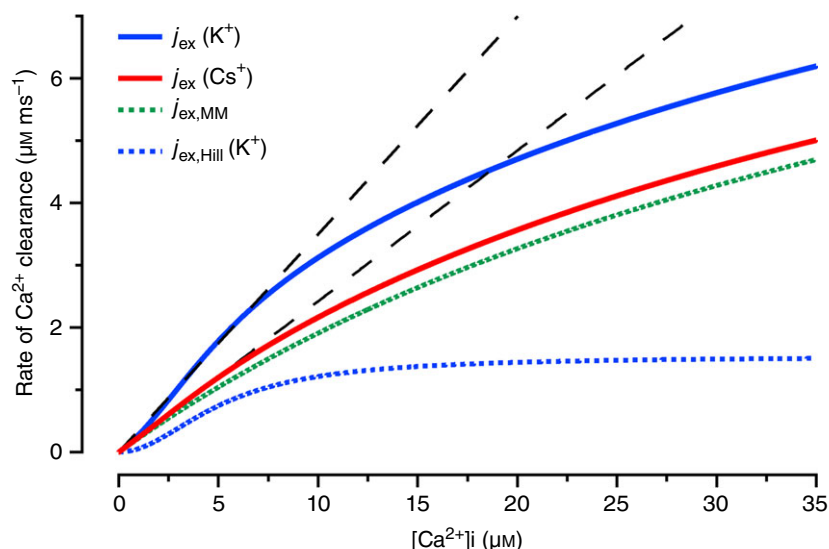
### Presynaptic voltage-gated $\text{Ca}^{2+}$ currents

Presynaptic voltage-activated  $\text{Ca}^{2+}$  currents at the calyx of Held have been described to display both facilitation and inactivation depending on the developmental stage and stimulation pattern (Cuttle *et al.* 1998; Forsythe *et al.* 1998; Borst & Sakmann, 1998b; Lin *et al.* 2011). When recording  $I_{\text{Ca}}$  evoked by 10–30 ms depolarizing voltage pulses with  $\text{Cs}^+$ -based pipette solutions at P13–15, we observed initial current facilitation (20–25% for AP-like stimuli at 200 Hz) followed by  $I_{\text{Ca}}$  inactivation. These changes, although small, markedly influenced the time course of the rising phase of  $[\text{Ca}^{2+}]_i$ , as evident when comparing simulations assuming constant  $I_{\text{Ca}}$  with those simulating the measured  $I_{\text{Ca}}$ . During our simulations we fitted  $I_{\text{Ca}}$  time courses by visual inspection (green traces in Figs 2A, C, E, 5 and 6), and modelled amplitude changes with two kinetic variables governing facilitation and inactivation (see Methods). The same set of  $I_{\text{Ca}}$ -related parameters was used for all model traces (see eqns 15–19 and Table 2), both for trains of AP-like stimuli and for

step depolarizations, with the exception that two different values were required for low- and high-EGTA traces regarding  $z_{\text{min}}$ , the lower bound of the inactivation variable (0.75 and 0.67, respectively).

Modelling  $[\text{Ca}^{2+}]_i$  transients yields an estimate of the accessible volume of the presynaptic terminal  $v$  (see eqns 4–6). Using  $\text{Cs}^+$ -based pipette solutions, we measured the isolated  $I_{\text{Ca}}$  together with the  $[\text{Ca}^{2+}]_i$  transients elicited by step depolarizations of three different durations (10, 30 and 50 ms). Estimates of  $v$  obtained from these experiments yielded  $0.30 \pm 0.01$  and  $0.46 \pm 0.02 \text{ pl}$  for the low-EGTA and high-EGTA experiments, respectively. The SEM values given here represent the variation between estimates from the three  $[\text{Ca}^{2+}]_i$  transients, each of which is an average obtained from five terminals. The difference between the  $v$  estimates obtained with either low-EGTA or high-EGTA pipette solution partially reflects differences in the size of the respective terminals (mean whole-cell capacitances were 21 and 23 pF) but may also include other influences.

When analysing these data, we first used an endogenous fixed buffer of 2.11 mM total concentration and a dissociation constant of  $100 \mu\text{M}$  ( $\kappa_s = 21.1$  at low  $[\text{Ca}^{2+}]_i$ ). We noted, however, that  $v$  estimates varied systematically when using step depolarizations of different durations, which elicited  $[\text{Ca}^{2+}]_i$  transients of very different amplitudes. For 50 ms long depolarizations ( $[\text{Ca}^{2+}]_i$  peak amplitude =  $40 \mu\text{M}$ ), the



**Figure 3. Presynaptic  $\text{Ca}^{2+}$  clearance rate as a function of cytosolic  $[\text{Ca}^{2+}]_i$**

$\text{Ca}^{2+}$  extrusion is modelled as a sum of two mechanisms: (i) a linearly rising, saturable component with Michaelis–Menten-type characteristics ( $j_{\text{ex,MM}}$ , green dotted trace) and (ii) a sigmoid mechanism with Hill-type characteristics ( $j_{\text{ex,Hill}}$ , blue dotted trace) (Lee *et al.*, 2007b). The two individual components  $j_{\text{ex,MM}}$  and  $j_{\text{ex,Hill}}$  are shown here for  $\text{K}^+$ -based pipette solutions. The solid traces represent the sum of the two components for either  $\text{K}^+$ -based (blue solid trace) or  $\text{Cs}^+$ -based (red solid trace) pipette solution. In the former case,  $j_{\text{ex,Hill}}$  is scaled up by a factor  $f_K = 4.79$  relative to its magnitude with  $\text{Cs}^+$ -based internal solution. Also shown are linear approximations to the total  $\text{Ca}^{2+}$  clearance rate under the two recording conditions (black dashed lines) for  $[\text{Ca}^{2+}]_i$  ranging from 0 to  $5 \mu\text{M}$ . These line fits are constrained to pass through the origin. For model parameters describing  $j_{\text{ex,MM}}$  and  $j_{\text{ex,Hill}}$  see Table 1 and the Results.



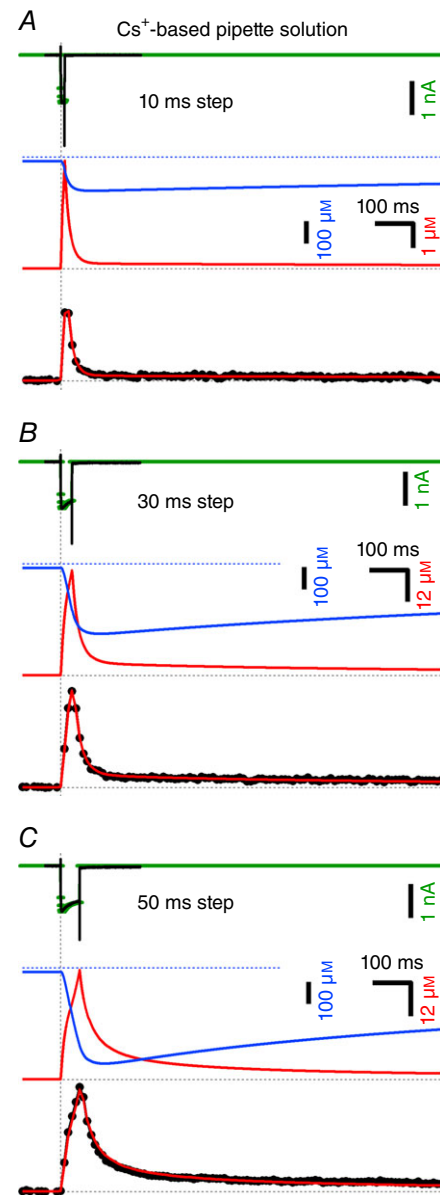
estimated  $\nu$  was 34% higher than that for 10 ms long depolarizations ( $[\text{Ca}^{2+}]_i$  peak amplitude =  $8.06 \mu\text{M}$ ). Such differences are unexpected, since the  $[\text{Ca}^{2+}]_i$  transients were recorded in the same terminals. We therefore hypothesized that the differences might be due to inappropriate assumptions about the affinity of endogenous fixed buffers and reanalysed these  $[\text{Ca}^{2+}]_i$  transients. We found that assuming a much lower  $\text{Ca}^{2+}$  affinity of the endogenous buffers ( $K_D = 400 \mu\text{M}$ ) results in similar  $\nu$  estimates for the  $[\text{Ca}^{2+}]_i$  transients obtained with the three different pulse durations. Therefore, we used this  $K_D$  value together with a total concentration of  $8.44 \text{ mM}$  (resulting in  $\kappa_s = 21.1$  at low  $[\text{Ca}^{2+}]_i$ ) for further analysis.

In our presynaptic  $I_{\text{Ca}}$  recordings we consistently observed small ( $\leq 50 \text{ pA}$ ), but in some cases long-lasting, inward currents following depolarizations. These slow tail currents tended to increase with the length of the depolarizations (typically  $-10$  and  $-20 \text{ pA}$  for 10 and 30 ms pulses). Although small, relative to the  $I_{\text{Ca}}$  peak amplitude measured during depolarizations ( $-1.0$  to  $-1.5 \text{ nA}$ ), these currents would delay the decay of  $[\text{Ca}^{2+}]_i$  transients after stimulation, if they actually reflected prolonged  $\text{Ca}^{2+}$  influx. Yet, an analysis of  $[\text{Ca}^{2+}]_i$  changes in the presence of EGTA argues against their  $\text{Ca}^{2+}$  specificity (see below), which led us to disregard the slow tail currents in our simulations.

### Presynaptic $[\text{Ca}^{2+}]_i$ dynamics in the presence of EGTA

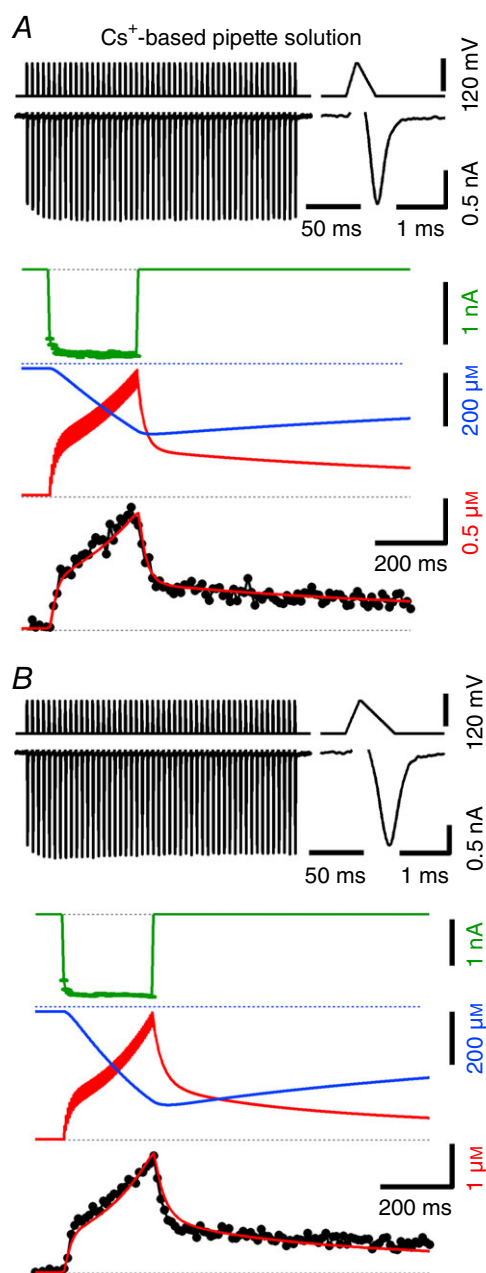
The  $\text{Ca}^{2+}$  chelator EGTA is often used to manipulate the  $[\text{Ca}^{2+}]_i$  dynamics in nerve terminals. In particular, its slower  $\text{Ca}^{2+}$  binding kinetics, as compared to the fast  $\text{Ca}^{2+}$  buffer BAPTA, are instrumental in probing the spatial relationships between  $\text{Ca}^{2+}$  sources and  $\text{Ca}^{2+}$  sensors (for a review see Eggermann *et al.* 2012). For such inferences, an accurate knowledge of the rate constants for  $\text{Ca}^{2+}$  binding and unbinding is essential. However, the literature for such quantitative data is ambiguous, with numbers for the rate constant of  $\text{Ca}^{2+}$  binding ranging between  $2.7 \times 10^6 \text{ M}^{-1} \text{ s}^{-1}$  (Naraghi & Neher, 1997; for  $\text{pH} = 7.2$ ) and  $1.05 \times 10^7 \text{ M}^{-1} \text{ s}^{-1}$  (Nägerl *et al.* 2000; for  $\text{pH} = 7.3$ ). Therefore, attempted to narrow down the plausible range for these important parameters. To this end, we performed experiments similar to those shown in Fig. 2A, C and E, except that we increased the concentration of EGTA by a factor of 10, including  $500 \mu\text{M}$  EGTA in the pipette. Figure 4A–C shows the measured and modelled  $[\text{Ca}^{2+}]_i$  transients. Basal  $[\text{Ca}^{2+}]_i$  is expected to be very low under these conditions (nominally  $\text{Ca}^{2+}$ -free pipette solution containing  $500 \mu\text{M}$  EGTA) and cannot be measured accurately with Fura-6F. We therefore assumed a basal  $[\text{Ca}^{2+}]_i$  of  $20 \text{ nM}$  and adjusted the baselines accordingly.

There are two obvious differences when comparing  $[\text{Ca}^{2+}]_i$  transients obtained with either 50 or  $500 \mu\text{M}$  EGTA



**Figure 4. Time course of  $[\text{Ca}^{2+}]_i$  transients in the presence of  $500 \mu\text{M}$  EGTA in the cytosol**

Similar experiment as illustrated in Fig. 2A, C and E but with a 10-fold higher EGTA concentration ( $500 \mu\text{M}$ ), using  $\text{Cs}^+$ -based pipette solution containing  $100 \mu\text{M}$  Fura-6F. The durations of the step depolarizations were 10 ms (A), 30 ms (B) and 50 ms (C). All recordings were obtained from the same set of presynaptic terminals ( $n = 5$ ). Measured  $I_{\text{Ca}}$  (top) and  $[\text{Ca}^{2+}]_i$  transients (bottom) are shown in black. The simulated  $I_{\text{Ca}}$  that was used to drive the model is shown in green. The predicted time course of the concentration of free EGTA is shown together with that of  $[\text{Ca}^{2+}]_i$  at high temporal resolution ( $\Delta t = 1 \text{ ms}$ ) in the middle row in blue and red, respectively. The bottom row shows modelled (red) and measured (black)  $[\text{Ca}^{2+}]_i$  transients superimposed. The modelled  $[\text{Ca}^{2+}]_i$  transient was binned using 10 ms time intervals that were shifted for optimal alignment with the measured trace. The measured peak  $[\text{Ca}^{2+}]_i$  was  $2.75 \mu\text{M}$  (A),  $6.03 \mu\text{M}$  (B) and  $9.32 \mu\text{M}$  (C). Model fits used 80 data points of the sampled  $[\text{Ca}^{2+}]_i$  trace starting at the onset of the presynaptic depolarization and ending 0.8 s later.



**Figure 5. Time course of  $[Ca^{2+}]_i$  transients in response to train stimulation in the presence of 500  $\mu M$  EGTA in the cytosol**

Similar experiment as illustrated in Fig. 4 using  $Cs^+$ -based pipette solution containing 100  $\mu M$  Fura-6F and 500  $\mu M$  EGTA but stimulated with 200 Hz trains consisting of 50 AP-like waveforms (APWs). The shape of the APWs was designed to approximate the time course of the recorded calyceal APs at P7 and P14 shown in Taschenberger & von Gersdorff (2000, their fig. 1A). A, narrow APWs that mimic mature calyceal APs were applied, which generate relatively small  $I_{Ca}$  ( $-1.38$  nA for the final  $I_{Ca}$ ). These APWs consisted of an initial ramp from  $-80$  to  $+40$  mV (200  $\mu s$ ), followed by a plateau at  $+40$  mV (40  $\mu s$ ) and finally a ramp from  $+40$  mV back to  $-80$  mV (360  $\mu s$ ). Measured  $I_{Ca}$  is shown in black (top left) together with the voltage-clamp train protocol. The first  $I_{Ca}$  of the train is shown at a faster time scale (top right). The simulated  $I_{Ca}$  that was used to drive the model is shown in green (middle). The predicted

in the pipette solution (Fig. 2A, C, E): (i) the maximum  $[Ca^{2+}]_i$  is greatly reduced and (ii) its decay is accelerated at higher  $[EGTA]_i$ , as expected for the chelating action of EGTA. In addition, there is another, albeit relatively subtle difference: a pedestal of elevated  $[Ca^{2+}]_i$  which slowly decays over several seconds. This is also expected on the basis of the  $Ca^{2+}$  binding characteristics of a slow chelator, because  $Ca^{2+}$  ions bound to the latter during a transient  $[Ca^{2+}]_i$  elevation dissociate slowly thereafter, contributing a source of  $Ca^{2+}$  ions, which slowly diminishes, while free  $Ca^{2+}$  is removed from the cytosol. Amplitude and decay kinetics of this pedestal depend critically on the dissociation rate constant of EGTA and therefore provide constraints to that parameter.

We also examined  $[Ca^{2+}]_i$  transients elicited by 200 Hz trains consisting of APWs. Figure 5A and B shows average  $[Ca^{2+}]_i$  transients recorded from the same calyx terminal using two different stimulation strengths. In Fig. 5A, the APW was designed to simulate the brief presynaptic APs observed in P13–15 calyces (Taschenberger & von Gersdorff, 2000). This resulted in relatively small  $I_{Ca}$  with a  $Q_{Ca}$  of  $\sim 0.38$  pC for the initial APW. The  $[Ca^{2+}]_i$  transient rose rapidly during the first 5–10 APWs to a level of about 0.6  $\mu M$  at which the influx of  $Ca^{2+}$  was close to being balanced by  $Ca^{2+}$  extrusion and, more importantly, by  $Ca^{2+}$  binding to EGTA. Subsequently,  $[Ca^{2+}]_i$  kept rising slowly, while free EGTA decreased. At the end of the stimulus train, free  $[EGTA]_i$  was reduced to 50% of its initial value (blue dotted trace in Fig. 5A).

In Fig. 5B, APWs were designed to simulate the wider APs observed at younger calyces (P8–10). This resulted in larger  $I_{Ca}$  corresponding to a  $Q_{Ca}$  of 0.74 pC, in agreement with Borst & Sakmann (1998a). Correspondingly, the rise in  $[Ca^{2+}]_i$  at the beginning of stimulation was faster, reaching an intermediary plateau level. For these large currents, however,  $[Ca^{2+}]_i$  kept rising at an accelerating

time courses of the concentration of free EGTA and  $[Ca^{2+}]_i$  are shown at high temporal resolution ( $\Delta t = 1$  ms) in blue and red, respectively (middle).  $[Ca^{2+}]_i$  peaked at  $\sim 1.38$   $\mu M$  at the end of the train while free EGTA dropped to  $\sim 50\%$  of its initial value. The bottom row shows modelled (red) and measured (black)  $[Ca^{2+}]_i$  transients superimposed. The modelled  $[Ca^{2+}]_i$  transient was binned using 10 ms time intervals and shifted for optimal alignment with the measured trace. Eighty data points of the sampled  $[Ca^{2+}]_i$  transient from the start of the stimulus train up to 0.8 s later were included in the model fit. B, similar experiment as shown in A obtained from the same calyx terminals, except that wider APWs mimicking immature calyceal APs were applied which gave rise to a  $\sim 27\%$  larger  $I_{Ca}$  ( $-1.75$  nA for the final  $I_{Ca}$ ). These APWs consisted of an initial ramp from  $-80$  to  $+40$  mV (280  $\mu s$ ), followed by a plateau at  $+40$  mV (40  $\mu s$ ) and finally a ramp from  $+40$  mV back to  $-80$  mV (680  $\mu s$ ). Using this stimulus protocol,  $[Ca^{2+}]_i$  peaked at  $\sim 2.73$   $\mu M$  at the end of the train while free EGTA dropped to  $\sim 28\%$  of its initial value. In total, 54 data points from the start of the stimulus train up to 0.54 s later were included in the calculation of least-squares fits.

pace. Our simulations indicate that the reason for this late rise is increased depletion of free EGTA, or else 'escape' from  $Ca^{2+}$  buffering (blue trace in Fig. 5B, where minimum  $[EGTA]_i$  is 28% of the initial value). Following stimulation,  $[Ca^{2+}]_i$  drops rapidly to the level of the pedestal as observed after step-depolarization at which  $Ca^{2+}$  clearance is balanced by dissociation of  $Ca^{2+}$  from  $Ca^{2+}$ -bound EGTA.

After strong stimulation, the presynaptic  $I_{Ca}$  was sometimes trailed by a small and slow inward tail current reminiscent of the  $Ca^{2+}$ -activated current observed after  $Ca^{2+}$  uncaging via flash photolysis (Wölfel & Schneggenburger, 2003; their fig. 2). We were concerned that this slow tail current might influence the decay of  $[Ca^{2+}]_i$ , if it reflected small but prolonged influx of  $Ca^{2+}$  ions (see above). However, time courses and amplitudes of the tail currents argue against such contributions. For instance, in the trace for the 10 ms depolarizing pulse displayed in Fig. 4A, the slow tail current following  $I_{Ca}$  with a peak amplitude of  $-1.38$  nA decays from an initial value of  $\sim 12$  pA to nearly 0 pA within the first 100 ms after the depolarization. The pedestal  $[Ca^{2+}]_i$ , however, is maintained over at least 500 ms. The extended small plateau of  $[Ca^{2+}]_i$  is thus unlikely to be caused by the slow tail current. In the case of the 30 ms pulse the tail current is larger ( $\sim 26$  pA) and does not decay much during the recording period. We simulated the injection of a  $Ca^{2+}$ -specific current of such magnitude into the terminal and found that this changes the plateau of  $[Ca^{2+}]_i$  by 30%. This calculation shows that a tail current of such magnitude might contribute to the plateau, if it were  $Ca^{2+}$ -specific. However, we doubt that this is the case, since the plateau for the 10 ms trace (during which the tail current vanishes) can be fitted with the same set of parameters as used for fitting the 30 ms trace, in which the tail current persists. We therefore neglected the small tail currents in our simulations and assumed that they were not carried by  $Ca^{2+}$  ions (see also Wölfel & Schneggenburger, 2003).

## Discussion

We describe  $Ca^{2+}$  current and  $[Ca^{2+}]_i$  transient measurements at voltage-clamped calyx of Held terminals, recorded under three different ionic conditions of intracellular dialysis. We first determine the  $Ca^{2+}$  buffer ratio  $\kappa_s$  of the endogenous fixed. We go on to use  $Cs^+$ -based as well as  $K^+$ -based pipette solutions supplemented with a minimal amount of EGTA and  $100 \mu M$  Fura-6F. Applying variable length depolarizations to elicit  $Ca^{2+}$  influx, we determine the kinetic parameters and  $Ca^{2+}$  dependence of  $Ca^{2+}$  clearance mechanisms under both ionic conditions, confirming previous results that  $Ca^{2+}$  clearance is faster in the presence of intracellular  $K^+$  compared to recordings with  $Cs^+$  as the main intracellular

cation. Finally, we perform similar experiments with elevated EGTA concentrations (0.5 mM), which allows us to determine the kinetic parameters of  $Ca^{2+}$  binding to and  $Ca^{2+}$  dissociation from this chelator.

Using this set of measurements, we determine the parameters defining  $Ca^{2+}$  influx,  $Ca^{2+}$  clearance and  $Ca^{2+}$  buffering, which will be discussed individually below. The parameters, which we determine by a joint least-squares fit to the entire data set are summarized in Table 1. Other parameters, in particular parameters resulting from a visual fit to  $I_{Ca}$  traces, are given in Table 2.

## Parameters related to $Ca^{2+}$ influx and endogenous buffering

We measured  $I_{Ca}$  both during voltage-step depolarizations of various durations as well as in response to trains of AP-like short stimuli. To aid  $[Ca^{2+}]_i$  modelling, we first derived parameters describing changes in  $I_{Ca}$  amplitudes during the various stimulus protocols by visual (trial and error) fits for best agreement between modelled and measured  $I_{Ca}$  shown in Figs 2, 4 and 5. Subsequently we used these  $I_{Ca}$ -related parameters (Table 2) to drive the  $[Ca^{2+}]_i$  model. The time constants describing relaxation of  $I_{Ca}$  facilitation (23 ms) and recovery from  $I_{Ca}$  inactivation (110 ms) are comparable to those derived experimentally for P8–10 calyces (Lin *et al.* 2012).

Simultaneous measurements of  $I_{Ca}$  together with the associated changes in  $[Ca^{2+}]_i$  allow one to obtain an estimate for the accessible volume  $v$  of the presynaptic terminal. Our  $v$  estimates (0.30 pl for the set of cells measured under low-EGTA conditions and 0.46 pl for cells under high-EGTA conditions) are similar to the previously reported value of 0.4 pl (Helmchen *et al.* 1997). As expected, they are somewhat less than the estimated total calyx terminal volume (0.48–0.71 pl; Sätzler *et al.* 2002; Vasileva *et al.* 2012). It should be pointed out, however, that in the model equations all fluxes are divided by the factor  $(1 + \kappa_B + \kappa_S)$ . Thus, any error in the latter will lead to an error in the scaling of the fluxes, compensating for the former error. For the case of  $j_{in}$ , which for a given  $I_{Ca}$  is inversely proportional to  $v$ , an underestimate of  $\kappa_S$  will lead to a concomitant overestimate of  $v$ . Also, a false assumption regarding the affinities of the fast buffers will lead to an apparent  $Ca^{2+}$  dependence of  $v$  (see also below). Such errors are not included in our error estimates for other fitting parameters, since we assumed a fixed  $\kappa_S$  for all simulations.

Our estimate for the endogenous fixed buffer ratio  $\kappa_S$  ( $= 21.1$ ; range 13–29) does contain a small contribution of mobile low-affinity  $Ca^{2+}$  binding species, contained in the pipette filling solution. While the contribution of the indicator dye is eliminated by the procedure of extrapolation to zero indicator dye (Fig. 1D, E) (Neher & Augustine, 1992), nucleotides and gluconate additionally

contribute to the measured value. According to the analysis of Woehler *et al.* (2014), these contributions amount to 1.8 and 1.75, respectively. Thus, the endogenous fixed buffers contribute only 17.55 to the estimated  $\kappa_s$ . However, all our measurements were performed with nucleotides and gluconate included in the pipette solution. So, for simplicity we assumed  $\kappa_s = 21.1$  for all calculations. The indicator dye was represented in the calculations, as described in the context of eqn (6).

### Parameters related to $\text{Ca}^{2+}$ clearance

The parameters given in Table 1 allow a detailed description of two  $\text{Ca}^{2+}$  clearance mechanisms as suggested by Lee *et al.* (2007b). We confirm their finding that a non-linear component of  $\text{Ca}^{2+}$  clearance mediated by a  $\text{K}^+$ -dependent Na/CaX speeds up  $\text{Ca}^{2+}$  clearance in the presence of intracellular  $\text{K}^+$ . However, optimal fitting required a lower affinity of  $j_{\text{ex,Hill}}$  ( $K_{\text{D,H}} = 5.16 \mu\text{M}$ ) than originally reported by Lee *et al.* (2007b;  $K_{\text{D}} = 1.7 \mu\text{M}$ ). This discrepancy may well be due to the use of different indicator dyes and discrepant assumptions about their dissociation constants. In particular, the type of analysis on which our  $K_{\text{D}}$  of Fura-6F is based yields a corresponding  $K_{\text{D}}$  for Fura-2FF of  $13.7 \mu\text{M}$  (Woehler *et al.* 2014), which is significantly higher than that derived by Lee *et al.* (2007b;  $3.1 \mu\text{M}$ ). Likewise, discrepancies in  $\gamma$  and  $j_{\text{H,max}}$  between our results and Lee *et al.* (2007b) are well taken care of by the different assumptions for indicator dye and  $\kappa_s$ .

### Kinetics of $\text{Ca}^{2+}$ binding to EGTA

The  $\text{Ca}^{2+}$  dissociation constant of EGTA, calculated from our kinetic parameters ( $K_{\text{D}} = k_{\text{E,Ca-}}/k_{\text{E,Ca+}} = 0.543 \mu\text{M}$ ), is 3.2 times higher than that obtained *in vitro*,  $0.171 \mu\text{M}$ , as calculated with the software Maxchelator (<http://maxchelator.stanford.edu/>) for pH 7.2 and an ionic strength of 190 mM. This is largely due to a higher dissociation rate constant of  $2.38 \text{ s}^{-1}$ . The latter, as calculated as the product of  $K_{\text{D}}$  and  $\text{Ca}^{2+}$  association rate constant, was reported to be  $0.5 \text{ s}^{-1}$  (Naraghi 1997) or else  $0.74 \text{ s}^{-1}$  (Nägerl *et al.* 2000). Also our  $\text{Ca}^{2+}$  association rate constant is faster than that determined by T-jump experiments (Naraghi & Neher, 1997) ( $2.7 \times 10^6 \text{ M}^{-1} \text{ s}^{-1}$ ), although it is slower than that determined by Nägerl *et al.* (2000) ( $1.05 \times 10^7 \text{ M}^{-1} \text{ s}^{-1}$ ). Part of the latter discrepancy is probably the result of a somewhat higher pH (7.3) and a lower ionic strength ( $\approx 150 \text{ mM}$ ) in the measurements of Nägerl *et al.* (2000). However, we attribute most of the discrepancies to different  $\text{Ca}^{2+}$  binding and unbinding rates of EGTA when measured either *in vitro* as in the previous studies or *in situ* as described here (see also discussion in Woehler *et al.* 2014).

### A consistent set of parameters for modelling $[\text{Ca}^{2+}]_i$ transients in a presynaptic CNS nerve terminal

To predict  $[\text{Ca}^{2+}]_i$  changes in response to voltage-clamp depolarizations or trains of APWs, a large number of parameters need to be known, as detailed at the beginning of the Results. Estimates for some individual parameters have been reported previously albeit for experiments conducted under a variety of different conditions (temperature, pH, ionic strength, developmental stage and type of nerve terminal). We made an effort to obtain a consistent and comprehensive set of parameters for the recording condition that is commonly used in studies at the calyx of Held. Apart from the determination of  $\kappa_s$ , which was done using younger calyces (P8–10), all our experiments were performed in P13–15 calyx terminals, at room temperature (20–23°C), and with pipette filling solutions of 190 mM ionic strength and a pH of 7.3. Furthermore, our measurements were all performed with the same  $\text{Ca}^{2+}$  indicator dye (Fura-6F), using a  $\text{Ca}^{2+}$  dissociation constant  $K_{\text{D}} = 17.8 \mu\text{M}$  (Woehler *et al.* 2014). This value is based exclusively on fluorescence measurements, performed using the same solutions as contained in recording pipettes, and does not rely on another  $\text{Ca}^{2+}$  buffer for calibration. Rather it uses a  $\text{Ca}^{2+}$  standard for titration. Nevertheless, it remains possible that the  $\text{Ca}^{2+}$  affinity of the indicator dye *in situ* is different from that *in vitro* (Tsien, 1983; Poenie, 1990) – just like we find for EGTA. Apart from this uncertainty about absolute  $[\text{Ca}^{2+}]_i$  values, our finding that one set of parameters accurately describes  $[\text{Ca}^{2+}]_i$  measurements covering a wide range of amplitudes and obtained using quite different stimulation protocols and ionic conditions, suggests that this set constitutes a sound basis for future studies of endogenous buffers and of the role of  $[\text{Ca}^{2+}]_i$  in synaptic plasticity.

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## Additional information

### Competing interest

The authors declare no competing financial interests.

### Author contribution

E.N. designed the study. K.H.L. performed experiments. K.H.L., H.T. and E.N. contributed to collection, analysis and interpretation of experimental data. E.N. performed numerical simulations and wrote the manuscript together with H.T. All authors have approved the final manuscript and agree to be accountable for all aspects of the work. All work was completed in the Department of Membrane Biophysics of the Max Planck Institute for Biophysical Chemistry.

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